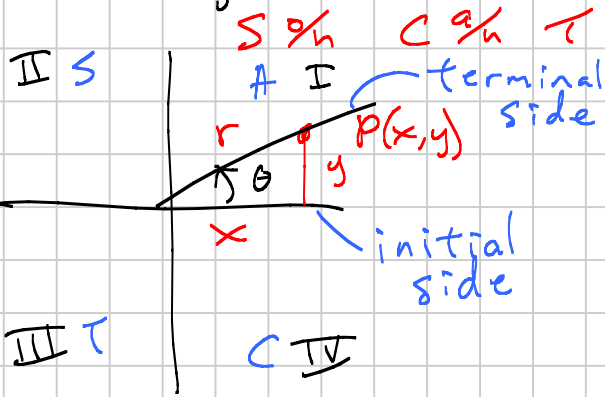


Pre Calc II Final Review Chp 6

Note Title

2016-05-25

6.1) Angles in Standard Position in Q I



$S \frac{y}{r}$ $C \frac{x}{r}$ $T \frac{y}{x} \Rightarrow S \frac{y}{r}$ $C \frac{x}{r}$ $T \frac{y}{x} = \text{slope}$.

+ive angle is CCW.
Use Pythagoras to determine missing side

$r = \sqrt{x^2 + y^2}$ $x = \sqrt{r^2 - y^2}$ $y = \sqrt{r^2 - x^2}$

Determine sign of x & y using ASTC or quadrant.

'r' is always positive.

For unit circle ($r=1$):

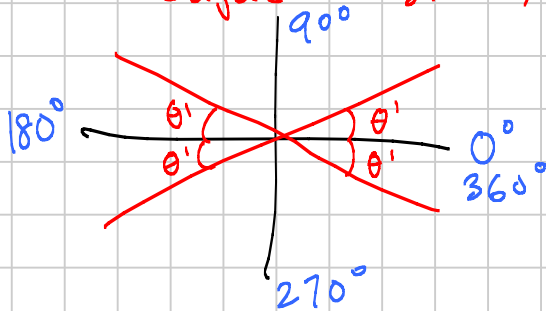
$y = \sin \theta$
 $x = \cos \theta$

For non-unit circle:

$y = r \sin \theta$
 $x = r \cos \theta$

6.2) Angles in Standard Position in All Quads.

Reference angle is measured from x-axis to the terminal side and is positive. This makes the adjacent side, the x-axis, so standard position works.



Reference angle: $0^\circ \leq \theta' \leq 90^\circ$
(use prime notation ')

I: $\theta = \theta'$ $\theta' = \theta$
II: $\theta = 180^\circ - \theta'$ $\theta' = 180^\circ - \theta$
III: $\theta = 180^\circ + \theta'$ $\theta' = \theta - 180^\circ$
IV: $\theta = 360^\circ - \theta'$ $\theta' = 360^\circ - \theta$

Special Angles:
Ref Angle

0°
 30°
 45°
 60°
 90°

$\sin \theta$
0
 $\frac{1}{2}$
 $\frac{\sqrt{3}}{2}$
 $\frac{\sqrt{3}}{2}$
1

$\cos \theta$
 $\frac{1}{\sqrt{3}}$
 $\frac{1}{\sqrt{2}}$
 $\frac{1}{2}$
0

$\tan \theta$
0
 $\frac{1}{\sqrt{3}}$
1
 $\sqrt{3}$
undef.

Inverse Trig - do on |ratio|, gives ref angle θ' , then determine quad and calc θ .

eg) $\cos \theta = -1/2$

$\theta' = \cos^{-1}(|-1/2|) = 60^\circ$

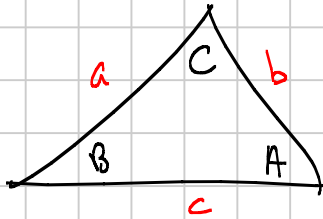
cos is negative in Q II & III

II: $\theta = 180^\circ - 60^\circ = 120^\circ$

III: $\theta = 180^\circ + 60^\circ = 240^\circ$

6.4) Sine Law:

$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$$



$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$

Put unknown variable in the numerator so that algebra is easier.

Case ASA: No checks, b/c not ambiguous.

After calculating 2nd angle, use triangle 180° property:

$$A + B + C = 180^\circ$$

Case ASS: Alternate method:

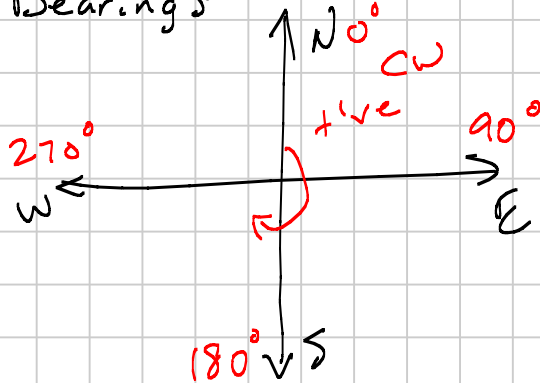
$a/c < \sin A$ - not a triangle.

$\sin A < a/c < 1$ - 2 triangles - ambiguous case.

$a/c \geq 1$ - 1 triangle.

With 2 triangles (ambiguous), the 2nd triangle is found by using the Q II formula: other C = 180° - C

Bearings



Alternate Bearing

dir → change → to dir

eg) N 20° E = 0° + 20° = 20°

E 30° N = 90° - 30° = 60°

S 15° W = 180° + 15° = 195°

Bearings

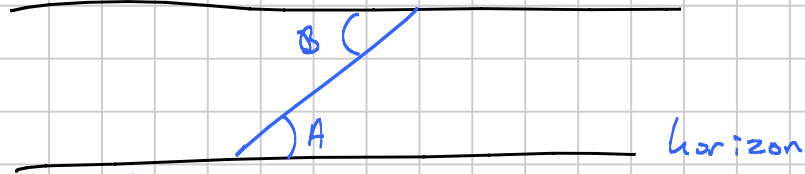
6.5) Cosine Law: - no ambiguous case

- use for SAS or SSS

$$c^2 = a^2 + b^2 - 2ab \cos C$$

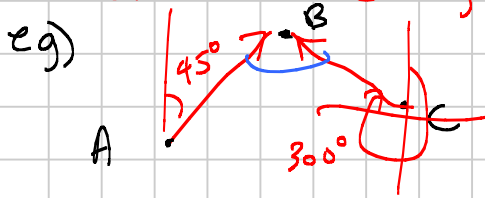
- only need to use once, then go with Sine Law & triangle property.

Definitions - Angle of Elevation (A), Angle of Depression (B)
inclination declination.



A & B are with respect to horizon.

When subtracting angles, make sure that you are using directions pointing away from the vertex. Reverse directions by adding/subtracting 180° (keep angles $0^\circ - 359^\circ$). If angle crosses 360° , add 360° to smaller direction before subtracting.



$$\begin{aligned} B \rightarrow A &= 45^\circ + 180^\circ = 225^\circ \\ B \rightarrow C &= 300^\circ - 180^\circ = 120^\circ \\ \angle B &= 225^\circ - 120^\circ = 105^\circ \end{aligned}$$