

PreCalc 12 Final Review Chp 1

Note Title

2016-05-27

1.1) Use long division if you are unsure about synthetic or not a monic linear binomial divisor. $(bx-a)$ $b=1$
For long or syn, pad missing powers "placeholders"
We need div to factor higher order polynomials and to calculate SA.

1.2 - Remainder Theorem (for $x-a$) $a \in \mathbb{R}$
Use $P(a)$ to calc remainder.

eg) $P(x) = x^3 + 2x^2 - 5x + 9$ $\leftarrow a_0$

$P(1) = 1 + 2 - 5 + 9 = 7$ is rem.

$P(-1) = -1 + 2 + 5 + 9 = 15$ is rem.

Use this mostly for Factor Theorem $P(a)=0$,
so $x-a$ is a factor of $P(x)$. Don't want
to do division to find factors. Then use
division to reduce polynomial to find more factors.

Use Factor Property to find potential 'a's. Start
with the small factors. $a_0 \in \mathbb{Z}$ - constant term

Use substitution when solving problems such as:

Find k when $P(x) = x^3 + kx^2 - 3x + 5$, $P(1) = 4$

Recall: Polynomial is $P(x) = a_n x^n + a_{n-1} x^{n-1} + a_{n-2} x^{n-2} + \dots + a_0$

1.3) Recall different odd/even definitions.

- numbers, degree, multiplicity, functions.

Multiplicity - # of times a root is repeated

- even (bounces), odd (goes thru) x -axis

- $(x-3)^2$ $(x+2)^5$

Degree - exponent of term with highest power

- even ($a_n > 0$ CU, $a_n < 0$ CD)

- odd ($a_n > 0$ III \rightarrow I, $a_n < 0$ II \rightarrow IV) leading coeff

- Degree is $>$ # of hills & valleys.

Also when graphing, graph y -int ($x=0$), and x -ints (if easy)

When using calculator, domain: use $-|a_0|, |a_0|$
(because factor prop)

1.4) Local/Global Min/Max - # < degree.
Functions - we're not solving (zeroes)
Equations - we're solving (roots)

1.5 - Know your formulas - review on your own.
Read carefully / highlight keywords.
Use answer as variable.
Create a function with relations (formulas)
- Substitute variable into relations.

Box - $V = lwh$
 $l = \frac{3}{2}w + 5$
 $h = \frac{4}{5}w - 4$) subst

$$V = \left(\frac{3}{2}w + 5\right)w\left(\frac{4}{5}w - 4\right)$$

Should only have one variable ↕